

Nesprávne a správne triangulácie

Bohdan Józsa

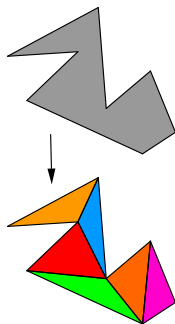
doc. RNDr. Andrej Ferko, PhD.

Katedra Informatiky
Fakulta Matematiky, Fyziky a Informatiky
Univerzita Komenského

Triangulácia

Neformálna definícia problému

Rozdeľ mnohoúholník na trojuholníky.



1911 Lennes, prvý algoritmus

1978 Garey, prvý algoritmus rýchlejší ako $O(n^2)$

1988 Tarjan a van Wyk, $O(n \log \log n)$

1990 Chazelle, lineárny algoritmus

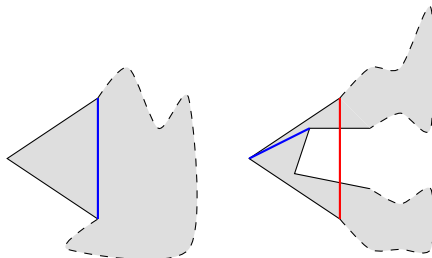
Každý mnohoúhelník s viac ako 3 vrcholmi obsahuje vnútornú diagonálu.

Toto umožňuje Divide & Conquer algoritmus:

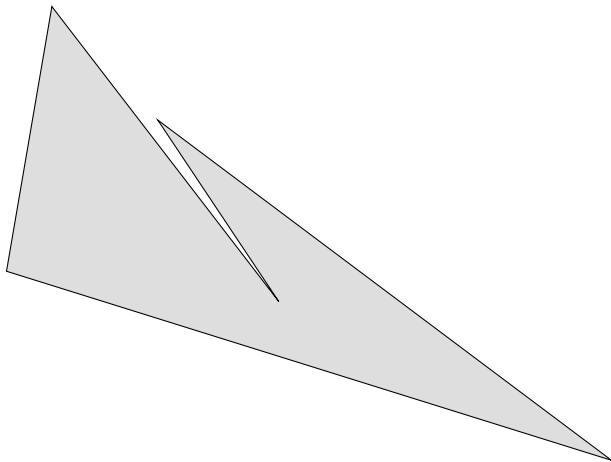
- 1 Nájdi nejakú vnútornú diagonálu
- 2 Rozdeľ ňou mnohoúhelník na dva nové
- 3 Rekurzívne ich trianguluj

Nájdí vnútornú diagonálu (Sellares, Toussaint)

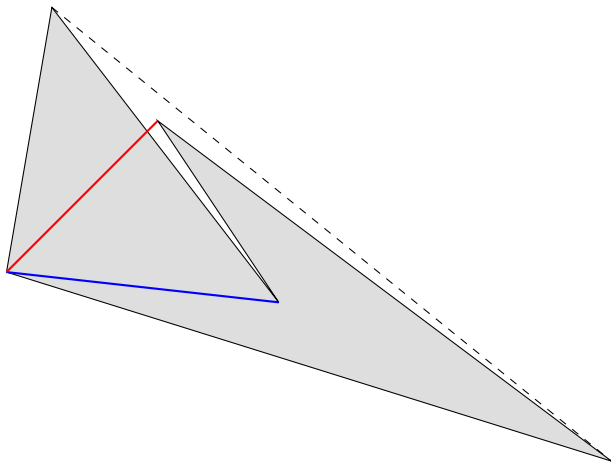
- 1 Nájdí konvexný vrchol
- 2 Ak jeho trojuholník neobsahuje ďalšie vrcholy, protiľahlá strana je diagonála
- 3 Inak jeden z vrcholov vnútri trojuholníka tvorí s vybratým vrcholom diagonálu



Minimálny protipríklad

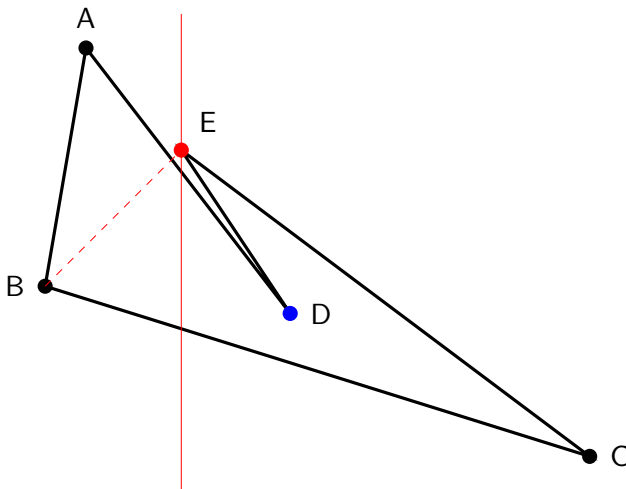


Minimálny protipríklad

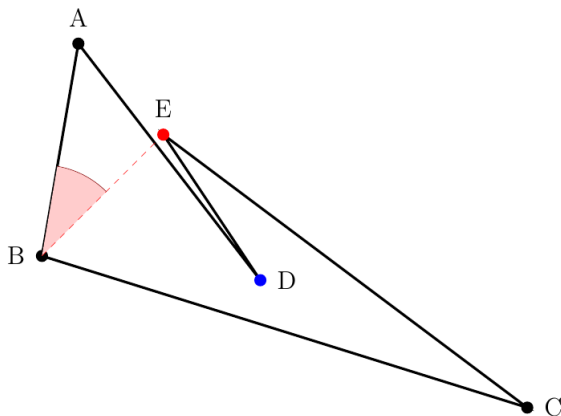


Nesprávne algoritmy

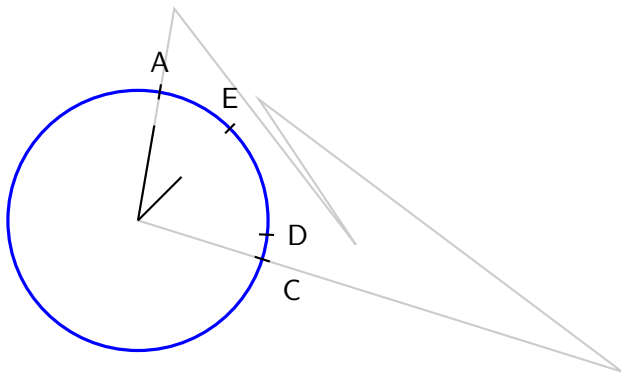
Zametanie zvislou čiarou (ten najľavejší)



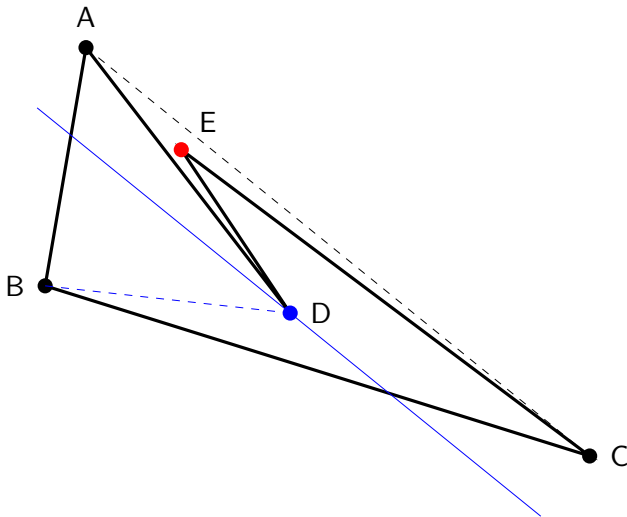
Zametanie rotujúcou čiarou okolo B



Metafora – hodiny

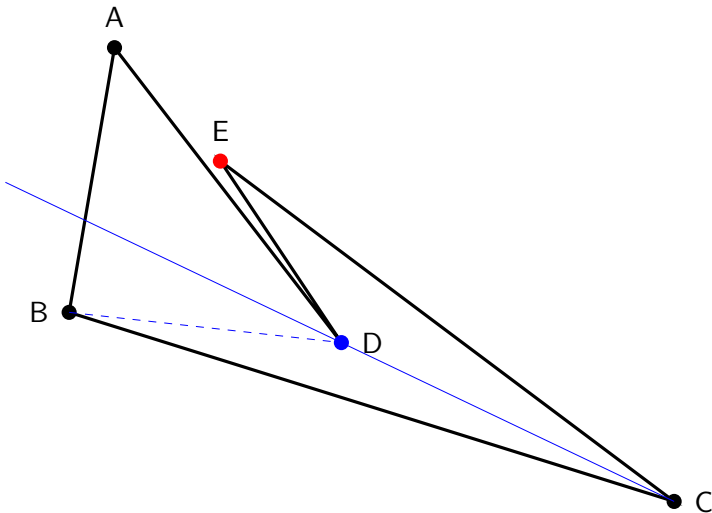


Správna translácia



Správna rotácia

Stred presunúť do C alebo A.



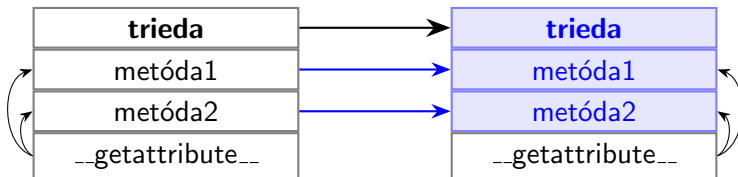
Vizualizácia

Jednoduchá vizualizácia algoritmov na mnohouholníkoch.

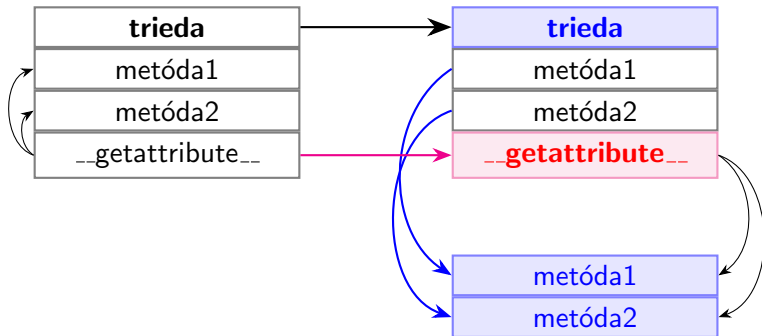
Ciele:

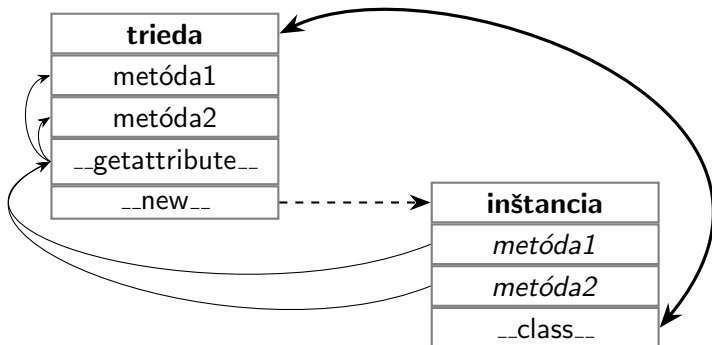
- jednoducho – bez drastických zmien v kóde algoritmu
- všeobecne – potenciálna možnosť vizualizovať iné druhy algoritmov

Dekorácia tried

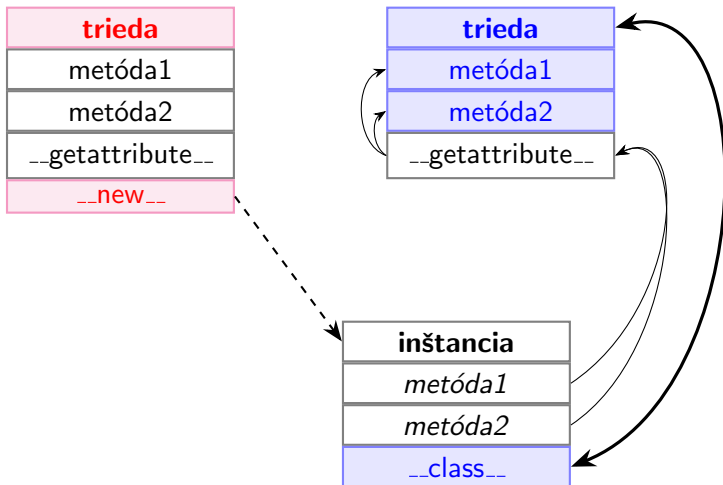


Dekorácia tried

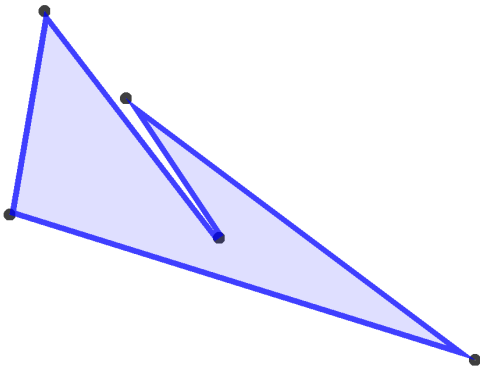




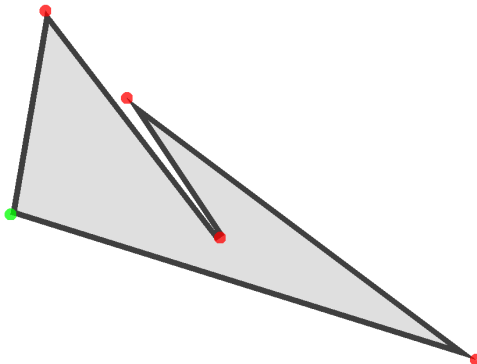
Transformovanie atribútov tried, aby zaznamenávali každé volanie.



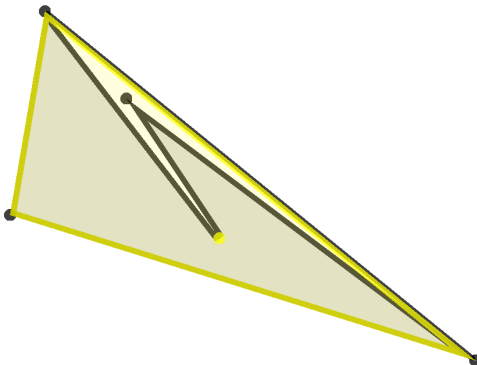
```
('polygon', [(1.0, 4.5), (9.0, 2.0), (3.0, 6.5), (4.6, 4.1), (1.6, 8.0)])  
__enter__(return)
```



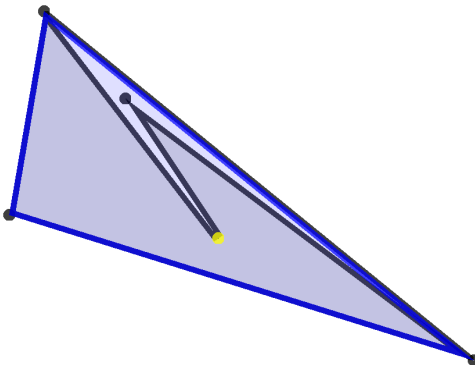
```
function call
left_most (return)
args
  ['Point2D(1, 9/2)', 'Point2D(9, 2)', 'Point2D(3, 13/2)', 'Point2D(23/5, 41/10)', 'Point2D(8/5, 8)']
Point2D(1, 9/2)
```



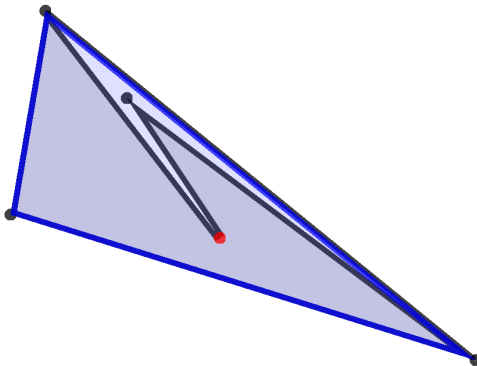
```
function call
is_inside (call)
args
  Point2D(23/5, 41/10)
  Triangle(Point2D(8/5, 8), Point2D(1, 9/2), Point2D(9, 2))
```



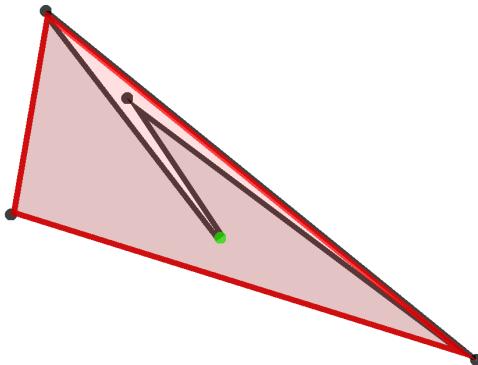
```
('polygon', [(1.6, 8.0), (1.0, 4.5), (9.0, 2.0)])  
encloses_point (call)  
args  
  Point2D(23/5, 41/10)
```




```
('polygon', [(1.6, 8.0), (1.0, 4.5), (9.0, 2.0)])  
encloses_point (return)  
args  
  Point2D(23/5, 41/10)  
True
```



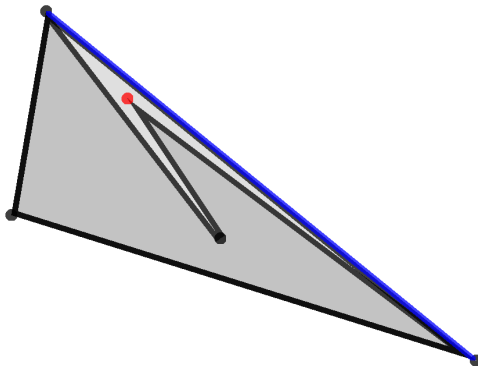
```
function call
is_inside (return)
args
  Point2D(23/5, 41/10)
  Triangle(Point2D(8/5, 8), Point2D(1, 9/2), Point2D(9, 2))
Point2D(23/5, 41/10)
```



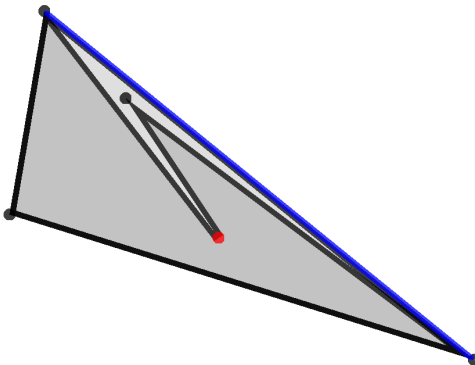
```

('segment', ((1.6, 8.0), (9.0, 2.0)))
distance (return)
args
  Point2D(3, 13/2)
27*sqrt(2269)/4538

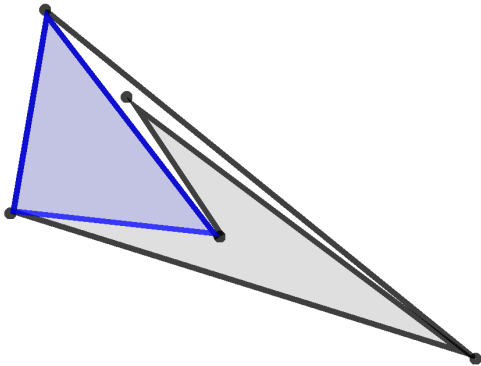
```



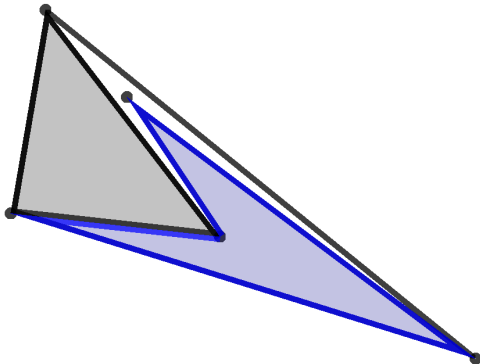
```
('segment', ((1.6, 8.0), (9.0, 2.0)))  
distance (return)  
args  
  Point2D(23/5, 41/10)  
543*sqrt(2269)/22690
```



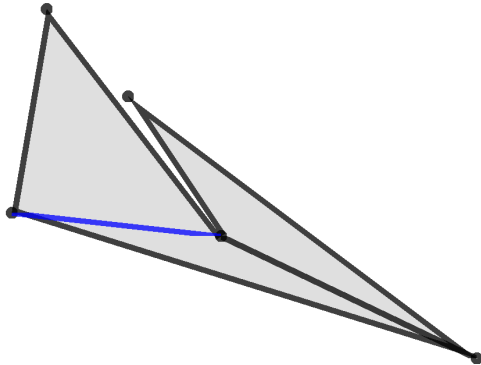
```
('polygon', [(1.0, 4.5), (4.6, 4.1), (1.6, 8.0)])  
__enter__(return)
```



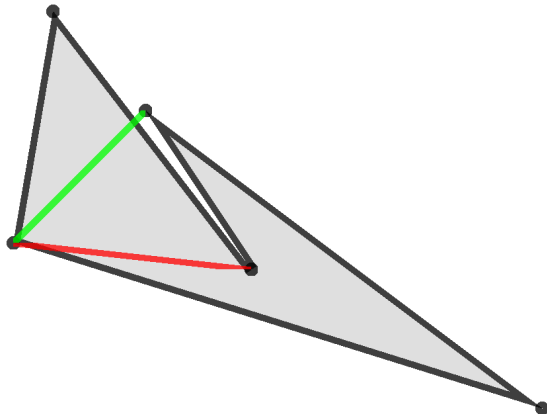
```
('polygon', [(1.0, 4.5), (9.0, 2.0), (3.0, 6.5), (4.6, 4.1)])  
__enter__(return)
```



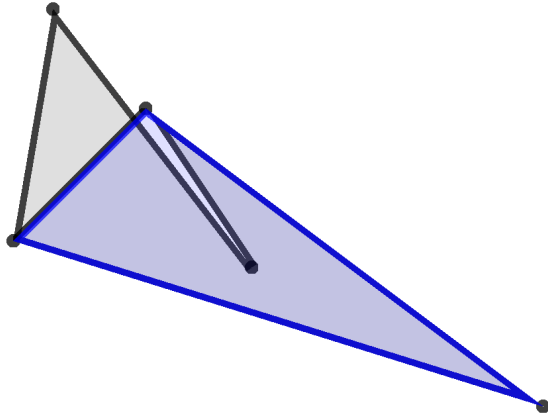
```
('segment', ((1.0, 4.5), (4.6, 4.1)))  
__enter__(return)
```



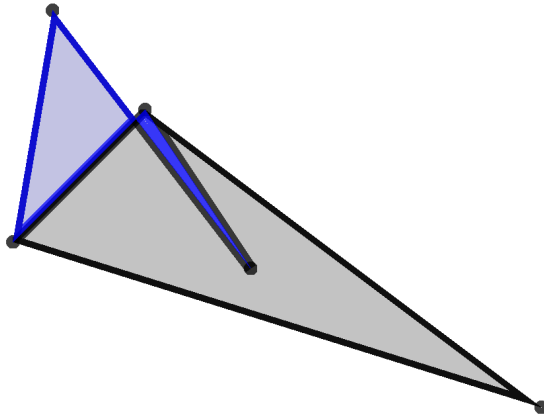
```
function call (return)
.compare_lengths
args
  Segment_2(PointC2(1, 4.5), PointC2(4.6, 4.1))
  Segment_2(PointC2(1, 4.5), PointC2(3, 6.5))
Segment_2(PointC2(1, 4.5), PointC2(3, 6.5))
```



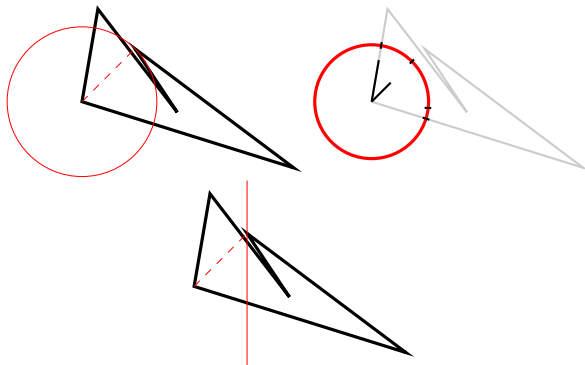

```
('polygon', [[1.0, 4.5], [9.0, 2.0], [3.0, 6.5]])  
.__enter__
```



```
('polygon', [[3.0, 6.5], [4.6, 4.1], [1.6, 8.0], [1.0, 4.5]])  
.__enter__
```



Vysvetlili sme problém triangulácie a niektoré nesprávne a správne riešenia.



Vytvorili sme prostredie na vizualizáciu algoritmov na mnohouholníkoch.